
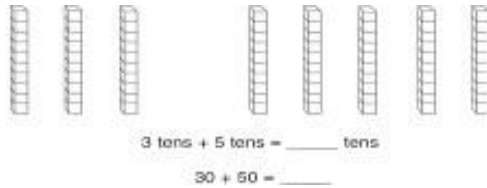
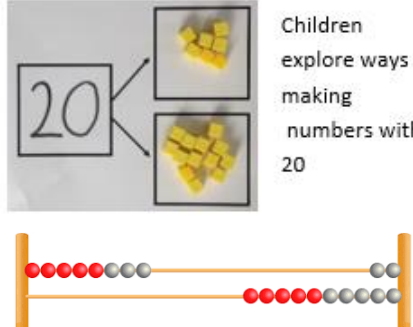
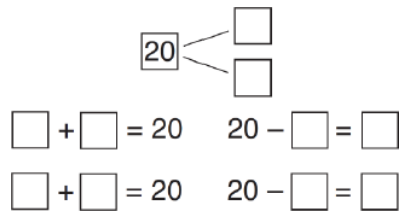

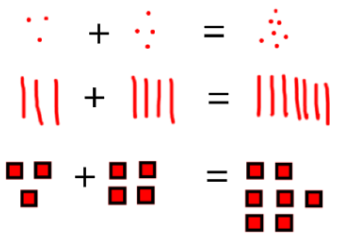


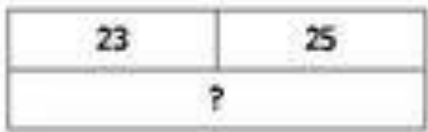
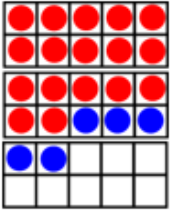
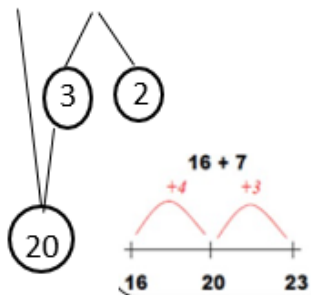
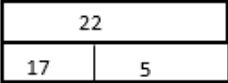
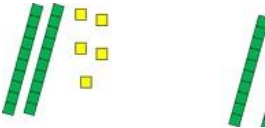
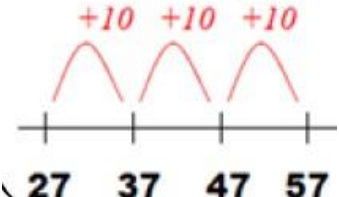
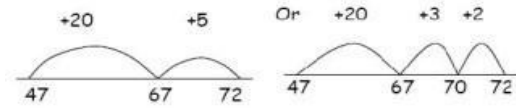


# Addition + Year 2

Objective & Strategy	Concrete	Pictorial	Abstract
Adding multiples of ten  Model using dienes and bead strings	$50 = 30 + 20$  Model using dienes and bead strings	 Use representations for base ten.	$20 + 30 = 50$ $70 = 50 + 20$ $40 + \square = 60$
Use known number facts  Part part whole	 Children explore ways of making numbers within 20	 $\square + \square = 20$ $20 - \square = \square$ $\square + \square = 20$ $20 - \square = \square$	$\square + 1 = 16$ $16 - 1 = \square$ $1 + \square = 16$ $16 - \square = 1$
Using known facts to build from		 Children draw representations of H,T and O	$3 + 4 = 7$ <i>leads to</i> $30 + 40 = 70$ <i>leads to</i> $300 + 400 = 700$

Bar model	 <p>Use actual objects to lay out in the formation of a bar model.</p> $3 + 4 = 7$	 <p>Use picture representations in the bar model. Turn the pictures into numbers.</p> $7 + 3 = 10$	 <p><math>23 + 25 = 48</math></p>
Add a two digit number and ones	 <p><math>17 + 5 = 22</math></p> <p>Use ten frame to make 'magic ten'</p> <p>Children explore the pattern.</p> $17 + 5 = 22$ $27 + 5 = 32$	<p>Use part part whole and number line to model.</p> <p><math>17 + 5 = 22</math></p> 	<p><math>17 + 5 = 22</math></p> <p>Explore related facts</p> $17 + 5 = 22$ $5 + 17 = 22$ $22 - 17 = 5$ $22 - 5 = 17$ 
Add a 2 digit number and tens	 <p><math>25 + 10 = 35</math></p> <p>Explore that the ones digit does not change</p>	<p><math>27 + 30</math></p> 	$27 + 10 = 37$ $27 + 20 = 47$ $27 + \square = 57$ $27$ $+ 10$ <hr/> $37$

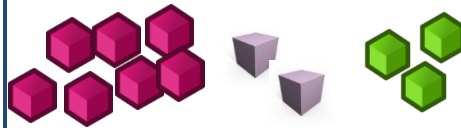
## Add two 2-digit numbers



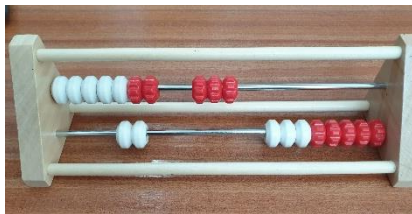
Use number line and bridge ten using part whole if necessary.

$$\begin{array}{r}
 25 + 47 \\
 \swarrow \quad \searrow \\
 20 + 5 \quad 40 + 7 \\
 20 + 40 = 60 \\
 5 + 7 = 12 \\
 60 + 12 = 72
 \end{array}$$

Add three 1-digit numbers



Combine to make 10 first if possible, or  
bridge 10 then add third digit.



Regroup and draw representation.

$$8 + 7 = 15$$

$$\begin{array}{l} \textcircled{4} + 7 + \textcircled{6} = \boxed{10} + \boxed{7} \\ \quad \quad \quad \underbrace{\hspace{1cm}}_{10} \\ \qquad \qquad \qquad = \boxed{17} \end{array}$$

Combine the two numbers that make/bridge ten then add on the third.

Reorder the digits to make adding easier.

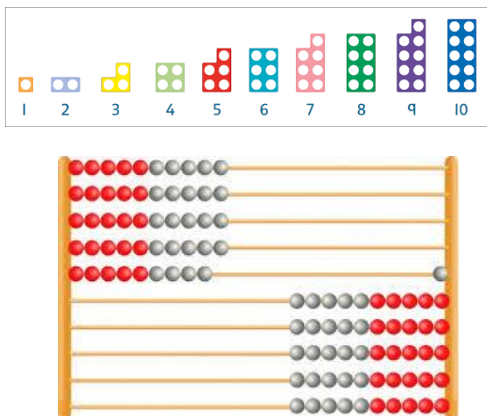

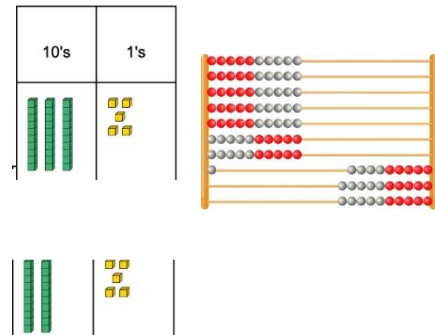
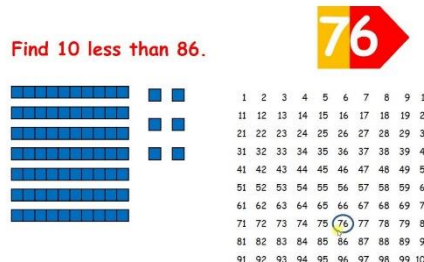
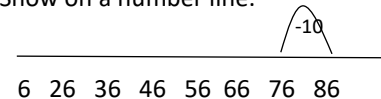
Partition a number to get to a ten to help with adding.

$$\begin{array}{r} 8 + 7 + 5 = \\ \quad \swarrow \searrow \\ \quad 2 \quad 5 \end{array}$$

$$8 + 2 + 5 + 5 =$$

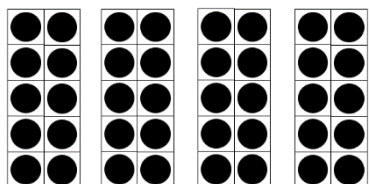
$$10 + 10 = 20$$

# Subtraction - Year 2

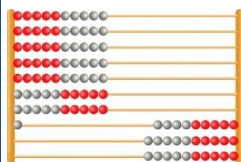
Objective & Strategy	Concrete	Pictorial	Abstract																																																																																																				
Subtract 1 / 1 less	<p>Use objects, numicon, rek n rek , dienes equipment to make a number and then show 1 less than.</p> 	<p>Use a 100 square to help find 1 less than a number. Discuss patterns seen.</p> <table border="1" data-bbox="1005 542 1268 769"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr><tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr><tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr><tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr><tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr><tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr><tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr><tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr></table> <p>Show on a number line.</p> 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	<p><math>18 - 1 = 17</math> <math>29 - \square = 28</math> <math>\square - 1 = 34</math></p> <p>Explore patterns and explain what can be seen happening in the numbers:</p> <p><math>60 - 1 = 59</math> <math>50 - 1 = 49</math> <math>40 - 1 = 39</math></p>
1	2	3	4	5	6	7	8	9	10																																																																																														
11	12	13	14	15	16	17	18	19	20																																																																																														
21	22	23	24	25	26	27	28	29	30																																																																																														
31	32	33	34	35	36	37	38	39	40																																																																																														
41	42	43	44	45	46	47	48	49	50																																																																																														
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91	92	93	94	95	96	97	98	99	100																																																																																														
Subtract 10 / 10 less	<p>Make using dienes equipment, beads strings, rek nrek.</p> 	<p>Use the 100 square to help find 10 less than a number. Discuss patterns seen.</p> <p>Find 10 less than 86.</p>  <p>Show on a number line.</p> 	<p><math>98 - 10 = 88</math> <math>47 - \square = 37</math> <math>\square - 10 = 63</math></p> <p>Explore patterns and explain what can be seen happening in the numbers:</p> <p><math>78 - 10 = 68</math> <math>68 - 10 = 58</math> <math>58 - 10 = 48</math></p>																																																																																																				

Subtract ones  
from a 10s  
number

Use 10s frames.



Use bead strings, rek n rek.



Use a 100 square. Count backwards from a 10s number.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90

$$60 - 7 = 53$$

$$80 - \square = 71$$

$$\square - 8 = 22$$

Explore patterns and explain what can be seen happening in the numbers:

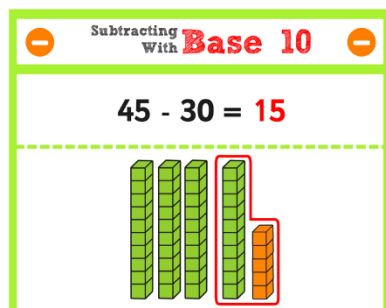
$$60 - 9 = 51$$

$$60 - 8 = 52$$

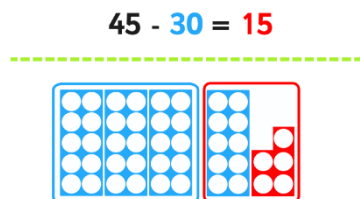
$$60 - 7 = 53$$

Subtract 10s

Use dienes equipment. Make the number and then subtract the 10s.



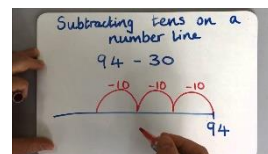
Use numicon to make the number and then subtract the 10s:



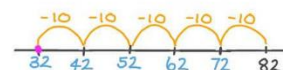
Work out using a 100 square.

Subtracting Multiples of 10									
$89 - 40 = 49$									
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Show on a number line.



Emma is subtracting on a number line.



Pick the calculation she is working on.

$$82 - 55$$

$$82 - 5$$

$$82 - 50$$

What is the answer? 32

$$87 - 30 = 57$$

$$95 - \square = 45$$

$$\square - 20 = 31$$

Explore patterns and explain what can be seen:

$$94 - 10 = 84$$

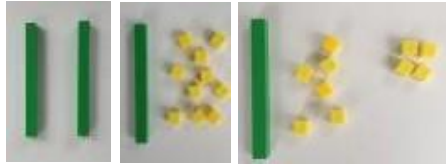
$$94 - 20 = 74$$

$$94 - 30 = 64$$

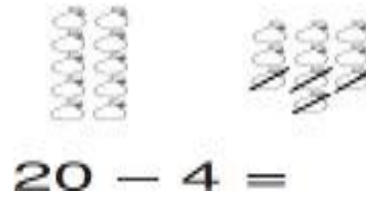
Column method

$$\begin{array}{r} 84 \\ - 30 \\ \hline 54 \end{array}$$

Regroup a ten into ten ones



Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'

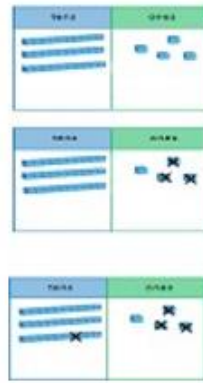


$$20 - 4 = 16$$

Partitioning to subtract without regrouping.

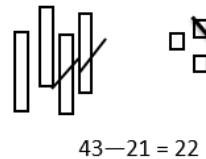
'Friendly numbers'

$$34 - 13 = 21$$



Use Dienes to show how to partition the number when subtracting without regrouping.

Children draw representations of Dienes and cross off.



Use a 100 square

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

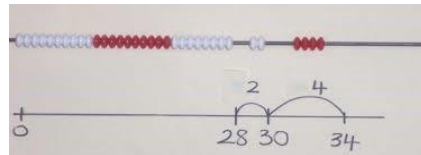
$$43 - 21 = 22$$

$$\begin{array}{r} 43 \\ - 21 \\ \hline 22 \end{array}$$

Subtracting across 10s.

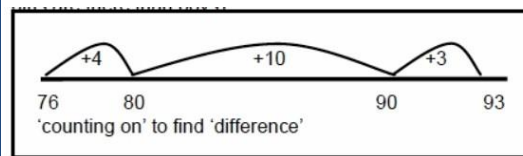
Make ten strategy

Progression should be crossing one ten, crossing more than one ten.



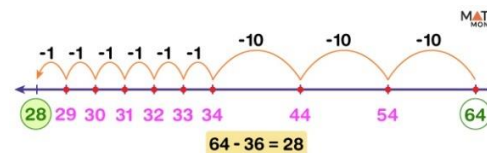
$$34 - 28$$

Use a bead bar or bead strings to model counting to next ten and the rest.



Use a number line to count on to next ten and then the rest.

Use the number line to count back the 10's, count back the 1's.



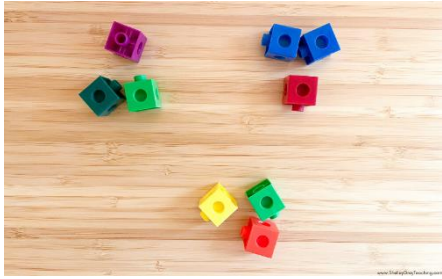


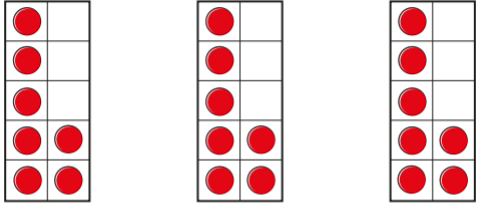
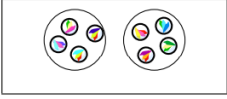


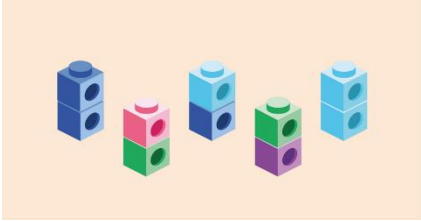

$$93 - 76 = 17$$

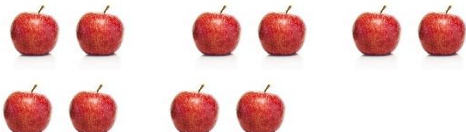
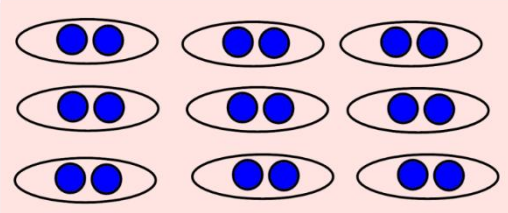

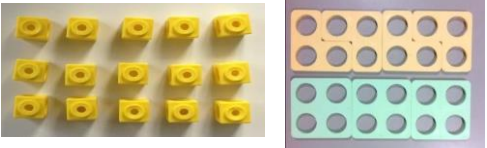
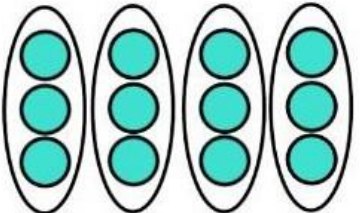
$$\begin{array}{r} 93 \\ - 76 \\ \hline 17 \end{array}$$



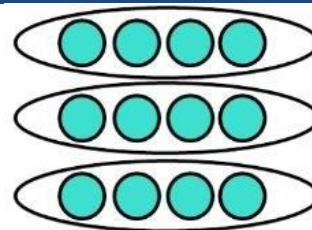
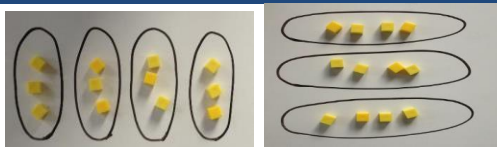
# Multiplication X

# Year 2

Objective & Strategy	Concrete	Pictorial	Abstract
Recognise and make equal groups	<p>Make equal groups using objects.</p>  	<p>Pictures of equal groups. Say what you can see.</p>   <p>There are <input type="text"/> equal groups with <input type="text"/> in each group.</p>	<p>There are 3 equal groups with 5 in each group.</p>  <p>There are 4 equal groups with 2 in each group.</p>  <p>There are 2 equal groups with 4 in each group.</p> 
Add equal groups	<p>Make equal groups using objects, dienes equipment, numicon.</p> <p>Count the objects made to find a total.</p> 	<p>Write a number sentence to match the picture.</p> 	<p>Max has five of the same coins. How much money does Max have if these are the coins?</p> <p>a) Max has five 1p coins. <input type="text"/> p</p> <p>b) Max has five 2p coins. <input type="text"/> p</p> <p>c) Max has five 5p coins. <input type="text"/> p</p> <p>d) Max has five 10p coins <input type="text"/> p</p>

<p>Multiplication sentences</p>	<p>Make groups using real objects, dienes, numicon, to help explore sentences that can be made.</p>  <p>5 groups of 2 apples equals 10 apples. 5 groups of 2 makes 10. 5 lots of 2 apples equals 10 apples. 5 apples multiplied by 2 apples equals 10 apples.</p>	<p>Use pictures of groups of objects to make up sentences. Draw groups.</p>  <p>9 groups of 2 equals 18. <math>9 \times 2 = 18</math></p>  <p><math>3 + 3 + 3 + 3 =</math> <input type="text"/>  <input type="text"/> lots of 3 = <input type="text"/>  <input type="text"/> <math>\times 3 =</math> <input type="text"/></p>	<p>5 lots of 2 = 10 5 groups of 2 = 10 <math>5 \times 2 = 10</math></p> <p>What is the same about the sentences? What is different?</p> <p>My answer is 12. What multiplication could it be?</p>
<p>Multiplication is commutative – Use arrays</p>	<p>Create arrays using counters and Numicon.</p>  <p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p>	<p>Use representations of arrays to show different calculations and explore commutativity. Draw the arrays themselves to explore calculations that can be made.</p> 	<p>Children to be able to use an array to write a range of calculations e.g.</p> <p><math>10 = 2 \times 5</math>  <math>5 \times 2 = 10</math>  <math>2 + 2 + 2 + 2 + 2 = 10</math>  <math>10 = 5 + 5</math></p>





Counting in multiples of 2, 5, 10 from 0  
(repeated addition)

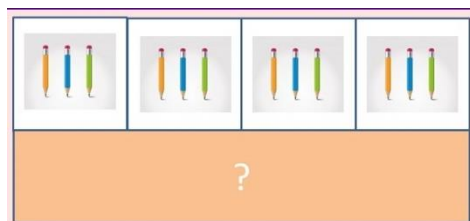
Count the groups as children are skip counting, children may use their fingers as they are skip counting.



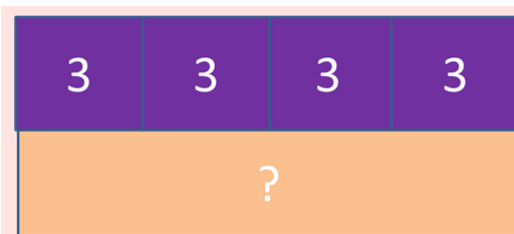
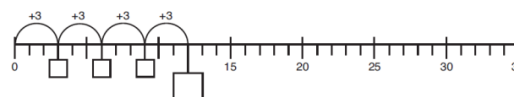
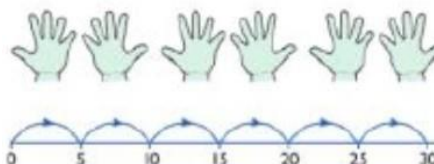
$$5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$$



Use concrete objects to make bar models



Number lines, counting sticks and bar models should be used to show representation of counting in multiples.



Count in multiples of a number aloud.  
Write sequences with multiples of numbers.

0, 2, 4, 6, 8, 10

0, 5, 10, 15, 20, 25, 30

Missing numbers in number patterns.

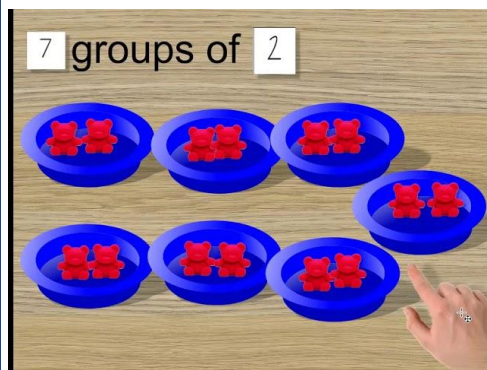
5 10 15 ? 25 30 35 ? 45 50

2 4 6 8 10 ? 14 16

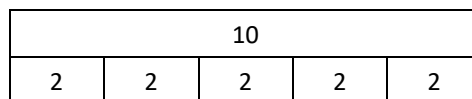
24 26 28 ? 32 34 36 ?

2, 5 and 10  
times tables

Use cubes, counters, objects to  
make equal groups of 2. Find the  
total.

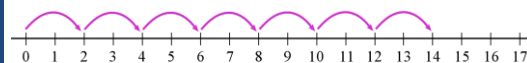


Bar models, number lines and pictures to  
represent 2 times table calculations.



$$2+2+2+2+2 = 10$$

$$5 \times 2 = 10$$



$$2+2+2+2+2+2 = 14$$

$$7 \times 2 = 14$$



$$\square \times \square = \square$$

$$5 \times 2 = 10$$

$$3 \times \square = 6$$

$$\square \times 2 = 14$$

$$3 \times 2 + 7 \times 2 = 20$$

Find different ways to  
make 20.

$$\square \times \square + \square \times \square$$

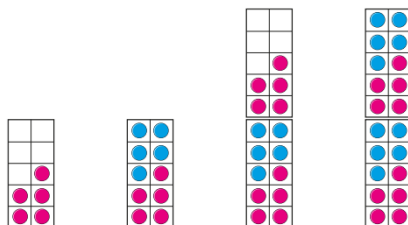
$$\square \times \square + \square \times \square$$

$$\square \times \square + \square \times \square$$

Making the link  
between the 5  
and 10 times  
tables

Make the 5 times table and 10 times  
table using tens frames and  
counters. Explore what is  
discovered. What numbers are in  
both?

a)



Use the 100 square to find patterns.

3 Here is a grid showing numbers from 51 to 100

51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

a) Colour the numbers that are in the  
10 times-table.

b) Circle the numbers that are in the  
5 times-table.

What do you notice?

5	10	15	20	25	30	35	40	45	50
10	20	30	40	50	60	70	80	90	20

What numbers are in both?

a)  $3 \times 10 = \square \times 5$

b)  $\square \times 10 = 2 \times 5$

c)  $5 \times 10 = \square \times 5$

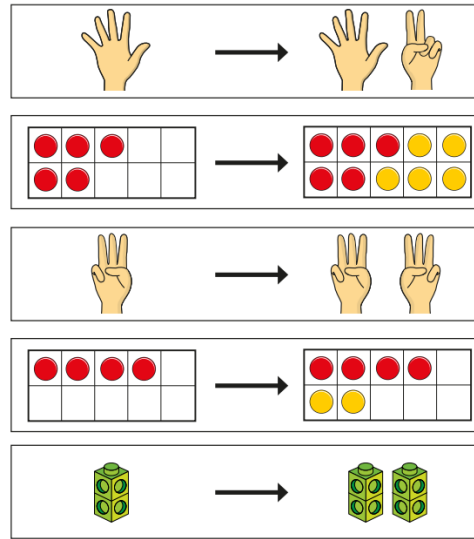
d)  $\square \times 10 = 12 \times 5$

## Doubling

Model doubling using dienes, objects and counters.



Which pictures show doubles?



Double 3 is equal to  $3+3$

Double 3 is equal to  $2 \times 3$

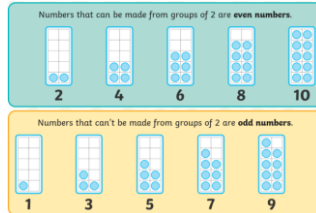
Double 3 makes 6.

Doubling a larger number: Partition a number and then double each part before recombining it back together.

$$\begin{array}{c} 16 \\ \swarrow \quad \searrow \\ 10 \quad 6 \\ \downarrow \times 2 \quad \downarrow \times 2 \\ 20 \quad + \quad 12 = 32 \end{array}$$

## Odd and even numbers

Use counters on 10s frames to make odd and even numbers.



Use numicon to show odd and even numbers.



Use a 100 square to mark on the odds and evens. Identify patterns.

EVEN & ODD NUMBERS									
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Mo is making a number pattern.

, 5, 7, 9, 11, 13, 15, ,

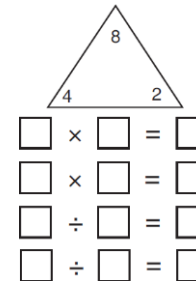
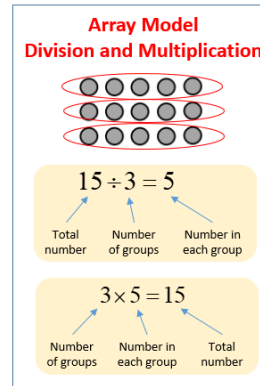
a) Write the missing numbers.

b) Write 2 numbers greater than 30 that could be in the pattern.

c) Write 2 numbers greater than 60 that could **not** be in the pattern.

Using the Inverse

*This should be taught alongside division, so pupils learn how they work alongside each other.*



$2 \times 4 = 8$

$4 \times 2 = 8$

$8 \div 2 = 4$

$8 \div 4 = 2$

$8 = 2 \times 4$

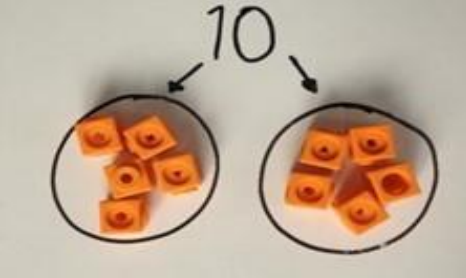
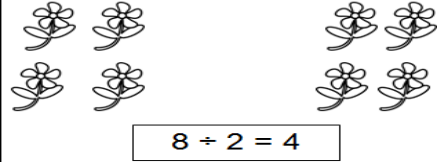

$8 = 4 \times 2$

$2 = 8 \div 4$

$4 = 8 \div 2$

Show all 8 related fact family sentences.

# Division ÷ Year 2

Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing  Focused teaching on division by 2,5,10.	 <p>I have 10 cubes, can you share them equally in 2 groups? <math>10 \div 2 = 5</math></p> <p>Use objects to physically sharing out between people.</p>	<p>Children use pictures or shapes to share quantities.</p>  <p><math>8 \div 2 = 4</math></p> <p>Children use bar modelling to show and support understanding.</p>  <p><math>12 \div 4 = 3</math></p>	$12 \div 4 = 3$ $16 \div \square = 8$ $\square \div 2 = 4$

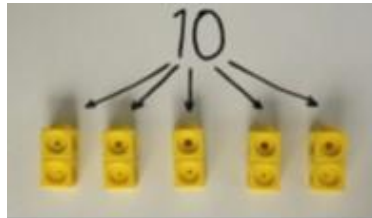
### Division as grouping

Focused teaching on division by 2,5,10.

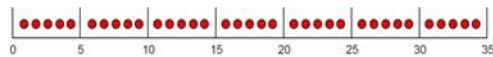
Divide quantities into equal groups.

Use cubes, counters, objects or place value counters to aid understanding.

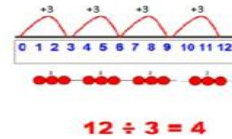
$$10 \div 2 = 5$$



$$35 \div 5 = 7$$



Use number lines for grouping



Use pictures to help make equal groups.

Mo has 20 chairs.



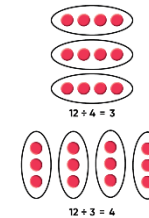
a) Circle groups of 5 chairs.

b) How many groups did you circle?

c) Complete the number sentence.

$$\square \div \square = \square$$

Using arrays



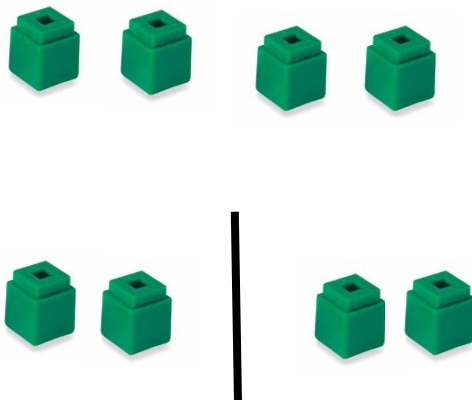
$$28 \div 7 = 4$$

$$24 \div \square = 12$$

Divide 28 into 7 groups. How many are in each group?

### Halving

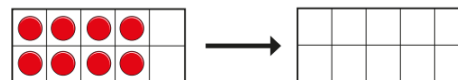
Model halving using dienes, objects and counters.



Use pictures to divide in half.



Draw the counters to show half.



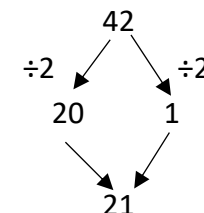
a) Half of 10 is equal to  ÷ 2

Half of 10 is equal to

b) Half of  is equal to 22 ÷ 2

Half of  is equal to

Halving bigger numbers.



Recombine to make the answer.

